Topological Methods in Nonlinear Analysis Journal of the Juliusz Schauder Center Volume 11, 1998, 375–395

## ON CLASSICAL SOLVABILITY OF THE FIRST INITIAL-BOUNDARY VALUE PROBLEM FOR EQUATIONS GENERATED BY CURVATURES

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Dedicated to Jürgen Moser

## 1. Main theorem and estimations in $\mathbb{C}^2$

The aim of this paper is to prove the existence theorem announced in [5]. The proof is based on  $\dot{a}$  priori estimates which were done in [6]–[8] for solutions to equations including the equations from [5]. We have to add to these estimates the estimates of Hölder constants for  $u_t$  and  $u_{x_ix_j}$ . Section 2 is devoted to this purpose.

We study the problems

(1.1) 
$$M_m[u] = 3D - \frac{u_t}{\sqrt{1+u_x^2}} + f_m(k[u]) = 3Dg \text{ in } Q_T = 3D\Omega \times (0,T),$$
  
(1.2)  $u = 3D\varphi \text{ on } \partial'Q_T, \ m \in [2,n],$ 

where  $\Omega$  is a bounded domain in  $\mathbb{R}^n$  with a smooth boundary  $\partial\Omega$ ,  $\partial'Q_T = 3D\partial''Q_T \cup \Omega(0)$ ,  $\partial''Q_T = 3D\partial\Omega \times [0,T]$ ,  $\Omega(0) = 3D\{z = 3D(x,t) \mid x \in \Omega, t = 3D0\}$ . Functions  $g : \overline{Q}_T \to \mathbb{R}^1$  and  $\varphi : \overline{\Omega} \to \mathbb{R}^1$  are known, and function

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<sup>1991</sup> Mathematics Subject Classification. 35J55.

Key words and phrases. fully nonlinear equations, evolution by curvature function, first initial boundary value problem, existence theorem.

The work of the first author was supported by RFFI grant 96-01-01199 and grant Nauch. Schools 96-15-96121; that of the second by RFFI grant 96-01-00824, grant Nauch. Schools 96-15-96121 and grant INTAS 96-835.