

## THE FORMAL THEORY OF SYLLOGISMS

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### 1. INTRODUCTION

By traditional logic is generally meant a whole body of theories that formed the realm of logic before contemporary logic was discovered by Frege. This logic is not strictly speaking Aristotle's theory, though it stemmed from Aristotle. Indeed it took also advantage of contributions by the Stoics and developed to a great extent during the Middle Ages and in modern times. It is certainly not limited to the theory of syllogisms, although this formed its core, at least in education.