

ERRATA
CORRECTION TO
DIRECT SUMMANDS OF DIRECT PRODUCTS
OF SLENDER MODULES

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Two corrections are necessary.

LEMMA 4.2. *Let I and T_1 be as given. Write $I = \bigcup_0^r I_k$, $k \in K$ an ordinal, where, for each $k < r$, I_k is finite and equals $\{i \in I \mid t_i \text{ is maximal in } T_1 \setminus \{t_i \mid i \text{ is in some } I_j \text{ with } j < k\}\}$ and where $\{t_i \mid i \in I_r\}$ contains no maximal element or an infinite number of maximal elements. If I_r is not empty, it contains an infinite chain $i_1 < i_2 < \dots$ such that, for each n , $t_i \not\preceq t_{i_n}$ when every $i_1 \leq i \leq i_n$ and $i \in I_r$.*

Proof of (4.3). In the first paragraph we change I_n to I_k . By factoring we may consider two cases. The case $I = I_r$ is like Case 1 in the paper. Consider the case where I_r is empty. For each k in K let $V_k = \prod_{j < k} (\prod_{I_j} R_i)$ and $V^k = \prod_{j \geq k} (\prod_{I_j} R_i)$. Now $V_k = A_k \oplus B_k$ with A_k in A and B_k in B . Also $A = A_k \oplus A^{k_j}$ where $A^k = A \cap (B_k \oplus V^k)$. Let $C_k = A_{k+1} \cap A^k$. For fixed i $\alpha_i(C_k) = 0$ for almost all k so $\prod_K C_k$ exists and is in A . If $a \in A$, we may find c_k in C_k for each k so that $a - \sum_{i < j} c_i \in A^j$ for each j . Now $a - \sum c_k \in \bigcap A^k \subseteq A \cap B$. So $a = \sum c_k$ and $A = \prod_K C_k$, a vector group.