

UNIQUENESS OF A CLASS OF STEADY PLANE GRAVITY FLOWS

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1. **Introduction.** In a previous communication [2] we established the existence of a class of free boundary flows of an incompressible inviscid fluid in a uniform gravitational field, having plane projections as illustrated in Figure 1. The flow domain is bounded on the right

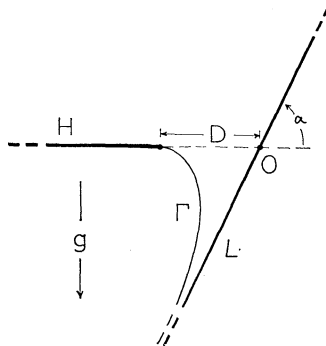


Fig. 1

by an infinite line L inclined at an angle α with the horizontal, and below and on the left by a semi-infinite horizontal line H and a free boundary arc Γ joined to H . The flow is downward through the slot between H and L into a jet bounded by L and Γ . The physical parameters include the boundary inclination α , the acceleration of gravity g , the slot width D , the area flow rate (flux) A , and the flow speed at the slot edge, q . It is shown in [2] that there exists a similarity class of such flows for each choice of the dimensionless pair α , gA/q^3 such that $0 < \alpha < \pi$, $0 < gA/q^3 < \infty$. The flows established there have convex free boundaries in the sense that their inclinations decrease monotonically from zero at the slot edge to $-\pi + \alpha$ at infinity, where they are asymptotic to the fixed boundaries L .

In this paper we shall establish the uniqueness of these similarity classes, find the ranges of the dimensionless products

$$(1.1) \quad \kappa = qD/A, \quad \lambda = gA/q^3, \quad \mu = gD/q^2, \quad \nu = gD^3/A^2$$

and determine the continuity and monotonicity relations between these products and other similarity invariants. (The products κ , λ , μ , ν are singled out since each involves only three of the four quantities g , D ,

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