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ERRATA
CORRECTION TO DENTABILITY, TREES, AND DUNFORD-PETTIS OPERATORS ON L_1

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A Banach space has the complete continuity property if all its bounded subsets are midpoint Bocce dentable. We show that a lemma used in the original proposed proof of this result is false; however, we give a proof to show that the result is indeed true.

1. Introduction. Throughout this paper, $\mathfrak{X}$ denotes an arbitrary Banach space, $\mathfrak{X}^*$ the dual space of $\mathfrak{X}$, $B(\mathfrak{X})$ the closed unit ball of $\mathfrak{X}$, and $S(\mathfrak{X})$ the unit sphere of $\mathfrak{X}$. The triple (Ω, Σ, μ) refers to the Lebesgue measure space on $[0, 1]$, Σ^+ to the sets in Σ with positive measure, and L_1 to $L_1(\Omega, \Sigma, \mu)$. The σ-field generated by a partition π of $[0, 1]$ is $\sigma(\pi)$. The conditional expectation of $f \in L_1$ given a σ-field $\mathscr{B}$ is $E(f|\mathscr{B})$.

A Banach space $\mathfrak{X}$ has the *complete continuity property* (CCP) if each bounded linear operator from L_1 into $\mathfrak{X}$ is *Dunford-Pettis* (i.e. carries weakly convergent sequences onto norm convergent sequences). Since a representable operator is Dunford-Pettis, the CCP is a weakening of the Radon-Nikodým property (RNP). Recall that a Banach space has the RNP if and only if all its bounded subsets are dentable. A subset D of $\mathfrak{X}$ is *dentable* if for each $\varepsilon > 0$ there is x in D such that $x \notin \overline{\mathrm{co}}(\{y \in D\colon \ \|x - y\| \geq \varepsilon\})$. Midpoint Bocce dentability is a weakening of dentability. The subset D is *midpoint Bocce dentable* if for each $\varepsilon > 0$ there is a finite subset F of D such that for each x^* in $B(\mathfrak{X}^*)$ there is x in F satisfying:

$$\text{if } x = \tfrac{1}{2}z_1 + \tfrac{1}{2}z_2 \text{ with } z_i \in D \text{ then } |x^*(x - z_1)| \equiv |x^*(x - z_2)| < \varepsilon.$$

The following theorem is presented in **[G1]**.

THEOREM 1. *$\mathfrak{X}$ has the CCP if all bounded subsets of $\mathfrak{X}$ are midpoint Bocce dentable.*