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## **ON NON-ELLIPTIC BOUNDARY PROBLEMS**

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## Introduction

The purpose of this paper is to study the boundary value problems for the second order elliptic differential equation

(1) 
$$AU = -\sum_{i,j=1}^{n} \partial_i (a_{ij}\partial_j U) + \sum_{i=1}^{n} b_i \partial_i U + cU = F$$

in a bounded domain  $\Omega$  in  $\mathbb{R}^n$   $(n \geq 3)$  with the boundary condition

(2) 
$$BU = \sum_{i=1}^{n} \alpha_i \partial_i U + \beta U = f$$

on the boundary  $\Gamma$  of  $\Omega$ , where we assume that

1) for every  $x \in \Gamma$ , the inequality

$$\sum_{i=1}^n lpha_i(x)^2 > 0$$

holds,

2) let  $(n_1(x), \dots, n_n(x))$  be the exterior unit normal vector to  $\Gamma$  at x, then the subset of  $\Gamma$ ,

$$\Gamma_0 = \left\{ x \in \Gamma; \sum_{i=1}^n \alpha_i(x) n_i(x) = 0 \right\}$$

is a  $C^{\infty}$ -manifold of dimension n-2,

3) at every point  $x \in \Gamma_0$ , the *n*-vector  $(\alpha_1(x), \dots, \alpha_n(x))$  is not tangent to  $\Gamma_0$ .

Here  $\partial_i$  denotes  $\partial/\partial x_i$ ,  $a_{ij}$  is symmetric on  $\Omega$ , and  $\Gamma$  is assumed to be infinitely smooth and of dimension n-1. We further assume that the coefficients of the equations (1) and (2) are real-valued and infinitely differentiable on  $\overline{\Omega} = \Omega \cup \Gamma$  and  $\Gamma$ , respectively, and that there exists a positive constant  $c_0$  such that

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