

## A SURVEY OF THE WORK OF GEORGE LUSZTIG

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### §1. Introduction

It is an honour to be invited to contribute a survey article on the work of George Lusztig in celebration of his 60<sup>th</sup> birthday.

George Lusztig came from the town of Timisoara in the mixed Romanian-Hungarian speaking part of Romania. He studied at the University of Bucharest and, after leaving Romania, worked with Michael Atiyah at the Institute for Advanced Study, Princeton for two years and also completed