

REMARKS TO THE UNIQUENESS PROBLEM OF MEROMORPHIC MAPS INTO $P^N(C)$, IV

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§1. Introduction

Let H_1, H_2, \dots, H_{N+2} be hyperplanes in $P^N(C)$ located in general position and $\nu_1, \nu_2, \dots, \nu_{N+2}$ divisors on C^n . We consider the set $\mathcal{F}(H_i, \nu_i)$ of all non-degenerate meromorphic maps of C^n into $P^N(C)$ such that the pull-backs $\nu(f, H_i)$ of the divisors (H_i) on $P^N(C)$ by f are equal to ν_i for any $i = 1, 2, \dots, N+2$. In the previous paper [6], the author showed that $\mathcal{F} := \mathcal{F}(H_i, \nu_i)$ cannot contain more than $N+1$ algebraically independent maps. Relating to this, the following theorem will be proved.

THEOREM. *The set \mathcal{F} is finite.*

We give here an example which shows that the number $\#\mathcal{F}$ of elements in \mathcal{F} is not less than $(N+1)!$. Take $N+1$ nowhere zero entire functions h_1, \dots, h_{N+1} such that $h_i/h_j \neq \text{const}$ if $i \neq j$, and define

$$F := h_1 + h_2 + \dots + h_{N+1}.$$

We consider hyperplanes

$$(1) \quad \begin{aligned} H_i &: w_i = 0 \quad (1 \leq i \leq N+1) \\ H_{N+2} &: w_1 + w_2 + \dots + w_{N+1} = 0 \end{aligned}$$

in $P^N(C)$ and divisors

$$\begin{aligned} \nu_i &= 0 \quad (1 \leq i \leq N+1) \\ \nu_{N+2} &:= \nu_F \end{aligned}$$

on C^n , where $w_1: w_2: \dots: w_{N+1}$ are homogeneous coordinates on $P^N(C)$ and ν_F denotes the divisor defined by the zero-multiplicity of F . Then, $\mathcal{F} := \mathcal{F}(H_i, \nu_i)$ contains

$$f^\sigma = h_{\sigma(1)}: h_{\sigma(2)}: \dots: h_{\sigma(N+1)}$$