

## Erratum

Kossakowski, A., Frigerio, A., Gorini, V., Verri, M.: Quantum Detailed Balance and KMS Condition. *Commun. math. Phys.* **57**, 97—110 (1977)

In the proof of Theorem 2.2, Equation (2.14) is wrong. To recover the correct proof, replace the part from line 1 after formula (2.13) (“Let  $H_N = \dots$ ”) to line -8 from the end of the proof (“...boundedness estimates”) by the following:

Let

$$C_{rr'ss'} = \frac{1}{2}(K_{rr'ss'} + K_{s's'r'r}Q_s Q_s^{-1}) = K_{rr'ss'} + i(\varepsilon_r - \varepsilon_s)\delta_{rr'}\delta_{ss'}$$

the equality of the two expressions following from Equation (2.13). By construction,  $\{C_{rr'ss'}\}$  satisfies (2.12), and moreover

$$\sum_{rr'ss'=1}^N C_{rr'ss'} P_{rr'} A P_{s's} = E_N \Psi E_N(A) + i[E_N(H), E_N(A)]$$

where  $E_N(A) = Q_N A Q_N$ ,  $Q_N = \sum_{r=1}^N P_{rr}$ .

Notice that  $E_N(A)$  converges ultraweakly to  $A$  as  $N \rightarrow \infty$ .

In particular, setting  $A = \mathbb{1}$ ,

$$\sum_{rr'ss'=1}^N C_{rr'ss'} P_{rr'} P_{s's} = E_N \Psi(Q_N)$$

which converges ultraweakly as  $N \rightarrow \infty$  to  $\Psi(\mathbb{1})$ , thus proving (2.11). Indeed,

$$\lim_{N \rightarrow \infty} \text{Tr} \{A_0 [E_N \Psi(Q_N) - \Psi(\mathbb{1})]\} = 0$$

for all  $A_0$  in the linear span of the  $P_{rs}$ 's, which is dense in the space of trace class operators on  $\mathcal{H}$ , and  $|\text{Tr} \{A_0 [E_N \Psi(Q_N) - \Psi(\mathbb{1})]\}|$  is bounded by  $2 \|A_0\|_1 \|\Psi\|$ .

Using the same kind of arguments, one proves that the expression

$$\begin{aligned} & \sum_{rr'ss'=1}^N C_{rr'ss'} (P_{rr'} A P_{s's} - \frac{1}{2} \{P_{rr'} P_{s's}, A\}) \\ & = E_N \Psi E_N(A) - \frac{1}{2} \{E_N \Psi(Q_N), A\} + iE_N([H, E_N(A)]) \end{aligned}$$

tends to  $L_s(A)$  ultraweakly as  $N \rightarrow \infty$ .

Finally, for any finite sequence  $\{x_{rr'}\}$  we have

$$\begin{aligned} & \sum_{rr'ss'=1}^N x_{rr'} C_{rr'ss'} x_{ss'} \\ & = \frac{1}{2} \sum_j \left\{ \left| \sum_{rr'} x_{rr'} \langle r | V_j | r' \rangle \right|^2 + \left| \sum_{rr'} y_{rr'} \overline{\langle r | V_j | r' \rangle} \right|^2 \right\} \geq 0, \end{aligned}$$

where  $y_{rr'} = x_{rr'} (\varrho_r \varrho_r^{-1})^{1/2}$  (we have used the fact that  $K_{rr'ss'} = 0$  if  $\varrho_r \varrho_r^{-1} \neq \varrho_s \varrho_s^{-1}$ ). The inequality clearly holds also for those infinite sequences for which the expression converges. This proves (2.10).