

Feynman Path Integrals

I. Linear and Affine Techniques II. The Feynman-Green Function

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Abstract. Path integrals techniques are derived from a new definition [1] of Feynman path integrals. These techniques are used to establish that Feynman-Green functions for a given physical system are covariances of pseudomeasures suitable for its path integrals. The variance of a pseudomeasure is a more versatile tool than the Feynman-Green function it defines.

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