

On Algebraic Equations Satisfied by Hypergeometric Correlators in WZW Models. I.

Boris Feigin¹, Vadim Schechtman,^{2,*} and Alexander Varchenko^{3,*}

¹ Landau Institute for Theoretical Physics, Moscow, Russia

² Dept. of Mathematics, SUNY at Stony Brook, Stony Brook, NY 11794, USA

³ Dept. of Mathematics, University of North Carolina at Chapel Hill, Chapel Hill, NC 27599, USA

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Abstract. It is proven that integral expressions for conformal correlators in $sl(2)$ WZW model found in [SV] satisfy certain natural algebraic equations. This implies that the above integrals really take their values in spaces of conformal blocks.

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1. Introduction

Let \mathbb{P}^1 be a complex projective line with a fixed coordinate z , $\mathbb{A}^1 = \mathbb{P}^1 - \{\infty\}$. Let \mathfrak{g} be a complex simple Lie algebra with a fixed invariant scalar product $(,)$ defining the symmetric invariant tensor $\Omega \in \mathfrak{g} \otimes \mathfrak{g}$, L_1, \dots, L_{n+1} its irreducible representations. Set

$$W = (L_1 \otimes L_2 \otimes \dots \otimes L_{n+1})_{\mathfrak{g}}.$$

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