

Moore and Seiberg's Equations and 3D Topological Field Theory

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Abstract. We prove that any solution to Moore and Seiberg's equations defines a Projective Rational Topological Field Theory (PRTFT) using surgery presentations for decorated three-manifolds and Kirby's calculus.

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