

## ON THE APPROXIMATION-SOLVABILITY OF EQUATIONS INVOLVING $A$ -PROPER AND PSEUDO- $A$ -PROPER MAPPINGS<sup>1</sup>

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### Table of Contents

#### Introduction

1.  $A$ -proper mappings and fixed point theorems for  $P_\gamma$ -compact mappings
  - 1.1 Basic facts about  $A$ -proper mappings and approximation-solvability
  - 1.2 Fixed point theory for  $P_\gamma$ -compact mappings
2. Equations involving linear  $A$ -proper mappings
  - 2.1 Approximation-solvability and bounded  $A$ -proper mappings
  - 2.2 Equations involving unbounded linear mappings
  - 2.3 Generalized Fredholm alternative
  - 2.4 Dirichlet boundary value problem for elliptic equations
  - 2.5 Stability of projective methods and  $A$ -properness
3. Equations involving nonlinear  $A$ -proper mappings
  - 3.1 Approximation-solvability and nonlinear  $A$ -proper mappings
  - 3.2 Equations involving odd  $A$ -proper mappings
  - 3.3 Alternative for asymptotically linear mappings with applications to PDE
4. Generalized degree theory of  $A$ -proper mappings and applications
  - 4.1 Definition and properties of the generalized degree
  - 4.2 Applications to some fixed point and mapping theorems
  - 4.3 Fréchet differentiable and analytic type  $A$ -proper mappings
5. Existence theorems and pseudo- $A$ -proper type mappings
  - 5.1 Equations involving pseudo- $A$ -proper mappings
  - 5.2 Application to fixed point and surjectivity theorems for  $G$ -operators,  $P_1$ -compact, weakly closed, and monotone type operators
  - 5.3 Equations involving uniform limits of  $A$ -proper type mappings
  - 5.4 Surjectivity theorems for odd limits of  $A$ -proper mappings

#### References

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