# ON A CLASS OF MINIMAL CONES IN $R^{n}$ 

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1. Introduction. In what follows let $S^{p}(\rho)=\left\{x \in R^{p+1}| | x \mid=\rho\right\}$ and $S_{p, q}=S^{p}\left((p /(p+q))^{1 / 2}\right) \times S^{q}\left((q /(p+q))^{1 / 2}\right) \subset S^{p+q+1}(1)$. Let $M$ be a codimension 1, closed minimal submanifold of $S^{n+1}(1)$ and $C(M)=\{t x \mid 0<$ $t<1, x \in M\}$.

It is well known that $C(M)$ is a minimal submanifold of $R^{n+2}$. An important question is whether $C(M)$ minimizes area in $R^{n+2}$ with respect to its boundary $M$. With respect to this question the following results are known:
(a) When $n \leqq 5$, Simons [4] has given a negative answer.
(b) When $M=S_{p, p}, p \geqq 3$, Bombieri-De Giorgi-Giusti [1] have given an affirmative answer.
(c) When $M=S_{p, q}$ and either $p+q \geqq 7$ or $p=q=3$ Lawson [2], using a different approach from Bombieri-De Giorgi-Giusti, has given an affirmative answer.
(d) Lawson has also proved that when $n=6$ or $n=7$ the set of minimal cones $C(M)$, that minimize area in $R^{n+2}$ with respect to their boundary $M$, is finite up to diffeomorphisms.

In this note we answer the question when $M=S_{p, q}$ with $p+q=6$.
2. Results. Using techniques related to those of Bombieri-De GiorgiGiusti, we were able to prove in [3] the following two theorems:

Theorem 1. If $p+q=n$ and either
(a) $n \geqq 7$ or
(b) $n=6$ with $|p-q| \leqq 4$,
then the cone $C\left(S_{p, q}\right)$ minimizes area in $R^{n+2}$ with respect to its boundary $S_{p, \alpha}$.

Theorem 2. $C\left(S_{1,5}\right)$ and $C\left(S_{5,1}\right)$ do not minimize area in $R^{8}$ with respect to their respective boundaries $S_{1,5}$ and $S_{5,1}$.

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