

# PERIODS OF INTEGRALS ON ALGEBRAIC MANIFOLDS: SUMMARY OF MAIN RESULTS AND DISCUSSION OF OPEN PROBLEMS

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