

RESEARCH ANNOUNCEMENTS

The purpose of this department is to provide early announcement of significant new results, with some indications of proof. Although ordinarily a research announcement should be a brief summary of a paper to be published in full elsewhere, papers giving complete proofs of results of exceptional interest are also solicited. Manuscripts more than eight typewritten double spaced pages long will not be considered as acceptable. All papers to be communicated by a Council member should be sent directly to M. H. Protter, Department of Mathematics, University of California, Berkeley, California 94720.

FUNCTIONAL INDEPENDENCE OF THETA CONSTANTS

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1. Introduction and main theorems. If

$$\begin{bmatrix} \epsilon \\ \epsilon' \end{bmatrix} = \begin{bmatrix} \epsilon_1 & \cdots & \epsilon_g \\ \epsilon'_1 & \cdots & \epsilon'_g \end{bmatrix}$$

is an even theta g -characteristic ($g \geq 1$ for this definition but $g \geq 2$ elsewhere in this note), i.e., a $2 \times g$ matrix with 0, 1 entries, for which $\epsilon \cdot \epsilon' \equiv 0(2)$ (dot is inner product of row g -vectors), and A is a symmetric $g \times g$ complex matrix with positive definite imaginary part, i.e., an element of the Siegel upper half plane \mathfrak{S}_g , then the corresponding theta constant is defined by

$$(1) \quad \theta \begin{bmatrix} \epsilon \\ \epsilon' \end{bmatrix} = \sum_n \exp \pi i \{ (n + \epsilon/2) A \cdot (n + \epsilon/2) + 2(n + \epsilon/2) \cdot (\epsilon'/2) \},$$

where the sum is over all integral row g -vectors n . There are $2^{g-1}(2^g+1)$ theta constants (explicit dependence on A is suppressed in the notation). These are the "zero values of the first order even theta functions with half-integer characteristics."

It is implicitly assumed, it seems to me, in the literature that the Jacobian of the $2^{g-1}(2^g+1)$ theta constants with respect to the $g(g+1)/2$ independent elements a_{ij} , $i \leq j$, $i, j = 1, \dots, g$ of A is generically of maximal rank $g(g+1)/2$ on \mathfrak{S}_g , but I have not seen a proof. I present here the sharper, i.e., explicit

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