$=0$ and $K L^{p}=L$ if and only if every finite-dimensional $L$-module is completely reducible. The latter implies that $\operatorname{Ext}_{V(L)}^{1}(M, N)=0$ for all $V(L)$-modules $M$ and $N$, finite dimensional or not, and therefore all $V(L)$-modules are projective and $V(L)$ has global dimension zero, i.e., $\operatorname{Ext}_{V(L)}^{n}(M, N)=0$ for all $n \geq 1$ and for all $M$ and $N$.

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# THE COHOMOLOGY OF THE STEENROD ALGEBRA; STABLE HOMOTOPY GROUPS OF SPHERES ${ }^{1,2}$ 

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In this paper, we state some of the results obtained by application of the methods of [4] to the study of the cohomology of the Steenrod algebra $A$. In brief, our results are a complete determination of $H^{s, t}(A)$ for $t-s \leqq 42$ in the $\bmod 2$ case, and for $t-s$ $\leqq 2(p-1)\left(2 p^{2}+p+2\right)-4$ in the $\bmod p$ case, $p>2$. Due to the existence of the Adams spectral sequence [1], these results give information about the stable homotopy groups of spheres.

We recall that the mod $p$ Adams spectral sequence $\left\{E_{r}\right\}$ (for the sphere) has differentials $\delta_{r}: E_{r}^{s, t} \rightarrow E_{r}^{s+r, t+r-1}$ and satisfies the properties:

$$
\begin{equation*}
E_{2}^{s, t} \cong H^{s, t}(A) \text { as a } Z_{p} \text {-algebra. } \tag{1}
\end{equation*}
$$

Each $E_{r}$ is a differential $Z_{p}$-algebra.
(3) $\left\{E_{\infty}^{s, t} \mid t-s=k\right\}$ provides a composition series for $\pi_{k}(S ; p$ ) (relative to a suitable filtration) ; here $\pi_{k}(S, p)$ denotes the stable homotopy group $\pi_{k}(S)$ modulo the subgroup of elements whose order is finite and prime to $p$.

[^0]
[^0]:    ${ }^{1}$ During the preparation of this paper, the author was partially supported by National Science Foundation grant number NSF-GP-1853.
    ${ }^{2}$ The work announced here is contained in the author's doctoral thesis, submitted to Princeton University.

