BOOK REVIEWS

University. His untimely death removes from the scene one of the early American workers in statistics.

J. Wolfowitz

Die Grundlagen der Quantenmechanik. By G. Ludwig. Berlin, Springer, 1954. 12+460 pp., 52 figures. Paperbound, 49 DM; clothbound, 52.60 DM.

This book gives a clear and interesting account of the quantum mechanics of a non-relativistic system with a finite number of degrees of freedom. This is a subject whose main lines, particularly consistency and uniqueness, are relatively well established. Roughly the first half of the book is devoted to a careful laying of the foundations of the subject from both the mathematical and physical sides. The second half develops the crucial applications and techniques in a thoroughgoing and readable way. The material of the book is well integrated and evenly presented, there being a good balance between the demands of intelligibility and those of brevity, with most doubtful situations being resolved in favor of the former. Though much of the mathematical and some of the physical material is essentially contained in von Neumann's well known book, the present work by its larger size and more limited scope provides a more spacious and elementary exposition. While its emphasis is on the physical side, its attitude is primarily logical, so that the mathematics is treated as a basic part of the scheme, rather than as a necessary evil. On the whole the book is solid and spirited, eclectic rather than pure, and should be unusually useful for some time to come.

The book includes somewhat condensed but readable treatments of Hilbert space and of group representation theory, in so far as they are used by it. Elsewhere in the book the mathematics makes use of assumptions that are generally clearly formulated so that the whole work is essentially quite rigorous. Important developments involving a relatively high level of mathematical sophistication are however omitted, among them von Neumann's theorem on the uniqueness of the Schrödinger operators and Kato's recent work in the Transactions on n-particle systems.

It is a significant anomaly that there is no material in this treatment of foundations on either quantum fields or relativistic invariance. The foundations that are presented are roughly as valid, from a physico-mathematical viewpoint, as the usual foundations of the Newtonian dynamics of a finite set of particles. Either theory is logically consistent as well as mathematically categorical and self-

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