1947]

 $\eta/a$  (the ratio of the length of the gap to the diameter of the antenna) and  $\eta/l$  (the ratio of the length of the gap to the length of the antenna). The classical sinusoidal current distribution is obtained in the limiting case where  $\eta/a$  is large and  $\eta/l$  is small. A general method of successive approximations is set up, but no proof of convergence

## is given. (Received October 31, 1946.)

of thick plates is discussed. (Received November 23, 1946.)

# Consider two thin circular discs of radius a with a common axis and at a distance d, d/a = q, charged to constant and opposite potentials, $V = \pm V_1$ . If the charges are $\pm Q$ , respectively, the constant $C = Q/V_1$ is called the capacity of the condenser. G. Kirchoff (*Cesammelte Abhandlungen*, p. 112) gave the following approximate formula for this important quantity: $a^{-1}C = (4q)^{-1} + (4\pi)^{-1} \log (1/q) + \alpha(q)$ , $\lim \sup \alpha(q) \leq (4\pi)^{-1} \cdot (\log (16\pi) - 1) = K \text{ as } q \rightarrow 0$ . Recently (Acad. des Sciences l'URSS, 1932) Ignatowsky gave the following sharper result: $\lim \alpha(q) = (4\pi)^{-1} (\log 8 - 1/2) = I$ . The proofs are in both cases somewhat incomplete. In the present paper Kirchoff's

78. Gabor Szegö: The capacity of a circular plate-condenser.

## 79. H. L. Turrittin: Stokes multipliers for asymptotic solutions of a certain differential equation.

proof is revised by using Dirchlet's principle. Moreover by means of the so-called Thomson principle a very simple proof is given for lim inf  $\alpha(q) \ge I$ . Finally the case

If v is a positive integer, the differential equation  $d^n y/dx^n - x^v y = 0$ ,  $n \ge 2$ , has n independent solutions  $y_j = x^j(1 + a_{1j}x^p + a_{2j}x^{2p} + \cdots + a_{mj}x^{mp} + \cdots)$ , p = v + n, convergent for all x. If the complex x-plane,  $x = re^{i\theta}$ , is divided into 2p sectors by the radial lines  $\theta = h\pi/p$ ,  $h = 0, 1, \cdots$ , Trjitzinsky (Acta Math. (1934) pp. 167-226) has shown that to each sector there corresponds n independent solutions  $\tilde{y}_k \sim \xi_k^{v(1-n)/2p} \exp \xi_k \{1 + b_1/\xi_k + b_2/\xi_k^2 + \cdots \}$  where  $\xi_k = (n/p)x^{p/n}e^{2\pi i k/n}$ . These asymptotic representations are valid uniformly throughout the sector (edges included). Therefore there exists a nonsingular linear relationship  $y_j = \sum_{k=0}^{n-1} c_{jk} \tilde{y}_k$ ,  $j = 0, 1, \cdots$ , n-1. These constants  $c_{jk}$ , which change from sector to sector, are the Stokes multipliers that have been computed. To do so the author borrowed heavily from the Ford-Newsom-Hughes theory of asymptotic expansion (Bull. Amer. Math. Soc. vol. 51 (1945) pp. 456-461). However this theory does not yield directly the desired uniform asymptotic representation in all cases, nor even the desired form when the real part of  $\xi_k$  is negative. The F-N-H theory is extended to supply the requisite information. Scheffé (Trans, Amer. Math. Soc. vol. 40 (1936) pp. 127-154) computed two of the n multipliers corresponding to each j. (Received October 7, 1946.)

### GEOMETRY

### 80. L. M. Blumenthal: Superposability in elliptic space. II.

Let f denote a one-to-one correspondence between the points of two subsets P, Q of the elliptic space  $E_{n,r}$ . Two corresponding subsets  $A_P$ ,  $B_Q$  of P, Q, respectively, are called f-superposable provided there exists a congruence  $\Gamma$  of  $E_{n,r}$  with itself which gives the same correspondence between  $A_P$  and  $B_Q$  as f does. The writer defines a space to have superposability order  $\sigma$  provided any two subsets of the space are superposable whenever a one-to-one correspondence f between the points of the subsets exists such that each two corresponding  $\sigma$ -tuples are f-superposable. A principal result of this paper is that  $E_{n,r}$  has minimum superposability order n+1. Two subsets