In fact if we let

$$T(n) = \sum_{\delta \mid n} F_{2\delta}$$

then

$$T(n) - 4T(n-1) + 11T(n-3) - 29T(n-6) + \cdots$$
  
= 
$$\begin{cases} (-1)^{k} kF_{2k-1} - F_{2k} & \text{if } n = k(k-1)/2 \\ 0 & \text{otherwise.} \end{cases}$$

Here the *m*th term of the sequence

1, 4, 11, 29, 76, 199, • • •

is

$$F_{2m} + F_{2m-2}$$

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## ON PARTICULAR SOLUTIONS OF LINEAR PARTIAL DIFFERENTIAL EQUATIONS

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1. Introduction. The boundary value and characteristic value problems are classical questions in the theory of partial differential equations of elliptic type. A method for actual solution of these problems consisting of approximations by expressions  $W_n = \sum_{\nu=1}^n \alpha_{\nu}^{(n)} \phi_{\nu}(x, y)$ , where  $\phi_{\nu}(x, y)$  are particular solutions of the considered differential equation, has been given by Bergman (see [1]).<sup>1</sup> Here the  $\alpha_{\nu}^{(n)}$  are constants which are to be determined by the requirement that the values of  $W_n$  on the boundary approximate the given data (for details see [1]).<sup>2</sup>

In applying this method it is important for practical purposes to obtain a simple procedure for the construction of the particular solu-

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<sup>&</sup>lt;sup>1</sup> The numbers in the brackets refer to the bibliography.

<sup>&</sup>lt;sup>2</sup> This method is in a certain sense the reverse of the Rayleigh-Ritz method in which the approximating expressions satisfy the boundary conditions but do not satisfy the given equation.