

$$ay^2 + by + c = dx^n,$$

$$a(b^2 - 4ac)d \neq 0, \quad n \geq 3,$$

has only a finite number of solutions as well as the equation

$$y^2 = ax^n + bx^{n-1} + \cdots + k$$

where, in the latter, the right-hand member has at least three different zeros.

After considering a number of special equations of the form

$$x^n + dy^n = \pm 1$$

where  $n=3$  or  $4$ , Skolem applies the theory of  $p$ -adic numbers to the equation

$$N(\alpha x + \beta y + \gamma z) = h$$

where  $\alpha, \beta$  and  $\gamma$  are integers in an algebraic field  $K$  of degree  $n$ . He finds equations of this type which have only a finite number of solutions for  $n=5$ .

We now signalize a problem which seems fundamental in this subject. If we consider the irreducible equation

$$f(x_1, x_2, \dots, x_k) = c$$

where  $f$  is of degree  $n$  with integral coefficients and with  $c$  integral and also  $f$  homogeneous we know from the theory of units in an algebraic field that for  $k=n$  and  $c=1$ , there exist equations of this type with an infinity of integral solutions. On the other hand, if  $k=2, n>2$ , Thue's theorem states that there cannot be more than a finite number of solutions. The question is, how far must  $k$  be increased to obtain equations of this type with an infinity of solutions? If  $n=3$ , we have  $k=3$ .

The arithmetical theory of Hermitian forms is not considered, likewise Waring's theorem. It is not exactly surprising that the latter topic has been omitted, as it would merit a volume in itself.

Skolem has written a very interesting book. It is surprising how much arithmetical meat he has packed into the space he employs.

H. S. VANDIVER

*Sur les Fonctions Orthogonales de Plusieurs Variables Complexes, avec les Applications à la Théorie des Fonctions Analytiques.* By Stefan Bergman. New York, Interscience Publishers, 1941. 62 pp. \$1.50.

This book was to appear as one of the *Mémorial des Sciences Mathématiques* series, but circumstances were such that the edition reached only the galley proof stage. The book is a photostatic edi-