## BRANCH-POINT MANIFOLDS ASSOCIATED WITH A LINEAR SYSTEM OF PRIMALS\*

## BY T. R. HOLLCROFT

1. Introduction. Linear  $\infty^{\alpha}$  systems of primals in  $S_r$  have been treated  $\dagger$  only for  $\alpha = 1$ , 2. The properties of a linear system are obtained from the characteristics of the jacobian and of the branch-point manifold associated with the system. There are, at present, no means for deriving most of the characteristics of a singular primal or manifold in  $S_r$ , especially for r > 4.

In this paper, a theorem is developed giving a set of characteristics of the branch-point manifolds of the system and its sub-systems. This is a step, not only toward the characterization of a general linear system in  $S_r$ , but also toward the study of singular manifolds which contain both nodal and cuspidal manifolds.  $\ddagger$ 

2. Definitions and Basic Considerations. In  $S_r$ , the linear  $\infty^r$  system,  $F_r$ , of primals is defined by the equation

(1) 
$$\sum \lambda_i f_i = 0, \quad (i = 1, 2, \dots, r+1),$$

in which the  $f_i$  are general algebraic functions of order n in the r+1 homogeneous variables  $x_i$ . Then  $f_i=0$  is the equation of a primal of order n without singularities in  $S_r$ .

The primals of  $F_r$  in the r-space (x) are in (1, 1) correspondence with the primes  $\sum a_i y_i = 0$ ,  $(i = 1, 2, \dots, r+1)$ , of an r-space (y). This correspondence is defined by the equations

$$\rho y_i = f_i, \quad (i = 1, 2, \dots, r+1).$$

<sup>\*</sup> Presented to the Society, September 12, 1935.

<sup>†</sup> T. R. Hollcroft, *Pencils of hypersurfaces*, American Journal of Mathematics, vol. 53 (1931), pp. 929-936; *Nets of manifolds in i dimensions*, Annali di Matematica, (4), vol. 5 (1927-28), pp. 261-267.

<sup>‡</sup> These terms will be used: node, a double point of a manifold at which the quadric hypercone is entirely general; nodal manifold of a manifold f, a manifold for every point of which (except points on pinch and singular loci) the two tangent linear manifolds to f are distinct; cuspidal manifold of f, a manifold for all points of which the two tangent linear manifolds to f coincide; cone to mean hypercone for r > 3.