

applied to the example discussed in these lines, is unknown. In fact it is not clear that there exist sets  $E$  for which  $H(E)$  is not vacuous. But it is obvious that  $H(E)$  is always contained in  $K(E)$ , where  $K$  is the set-function (assumed additive) in terms of which  $H$  is defined.

In the example in question it is true that an "accessible" topology can be defined in terms of neighborhoods in such a way that the function  $Lx_n$  defined in terms of these neighborhoods is identical with the original function  $L$ , and so that the set of all continuous functions is dense on the whole space.

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## ON (2, 2) PLANAR CORRESPONDENCES

BY L. H. CHAMBERS

1. *Introduction.* Most of the existing literature dealing with (2, 2) planar transformation is of the type given by the product of two harmonic homologies. By this I mean that the pairs of points of the plane  $\pi$  (or  $\pi''$ ) are in harmonic homology. Papers of this type were given by E. Amson,\* T. Kubota,† and P. Visalli.‡ Barraco§ defined an involutorial (2, 2) transformation of the plane by means of an involution between the tangents to a conic from points of the plane.

In this paper I shall consider only periodic (2, 2) transformations of period two. The treatment in each case, except those involving the Bertini involution, will be analytic. A synthetic treatment of some of the cases has been given by Sharpe and Snyder.|| I shall use the following theorems proved in their paper.

A necessary and sufficient condition that the two images of a point  $P$  describe distinct loci as  $P$  moves on a curve  $C$  is that  $C$  touches the branch curve at every non-fundamental point they have in common.

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\* Erlangen Dissertations, vol. 130 (1903-04).

† Science Reports, Tôhoku, vol. 6 (1918), and vol. 14 (1925).

‡ Circolo Matematico di Palermo, Rendiconti, vol. 3 (1889), pp. 165.

§ Giornale di Matematiche, vols. 53-54 (1915-16).

|| Transactions of this Society, vol. 18 (1918), pp. 409.