NOTE ON THE ORIENTATION OF A SECANT.

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In a previous paper * the orientation of curves and their tangents is briefly discussed. For certain problems in the theory of the potential function it is desirable to be able to define uniquely the positive sense along a secant through two variable points of an open smooth curve in such a way that the angle α between the positive direction of the secant and a fixed line shall be a continuous function of the two variable Such a definition will include the tangent as a special A natural method would be to define the positive sense uniquely and then prove that α is continuous. Another method would be to define the positive sense of the secant for one position and then define the positive sense in every other position so that the angle α shall be continuous. Either method involves somewhat troublesome considerations if the angle is defined by means of any one of the inverse trigonometric func-The method of defining an angle used in the paper above mentioned proves useful in this case.

Given the open curve

$$x = x(t), \quad y = y(t), \qquad \qquad t_0 \le t \le T,$$

where x, y, dx/dt, dy/dt are single-valued and continuous in the interval (t_0, T) , and where

$$x(t_1) \neq x(t_2), \quad y(t_1) \neq y(t_2) \quad \text{when } t_1 \neq t_2.$$

Define a secant through the points t_1 , t_2 as follows:

$$X = \epsilon \lambda \rho + x(t_1), \quad Y = \epsilon \mu \rho + y(t_1),$$

where ϵ is arbitrarily chosen either +1 or -1, ρ is the variable parameter, and

^{*&}quot;An arithmetic treatment of some problems in analysis situs," Amer. Jour. of Mathematics, Oct., 1905, p. 349.