

where

$$\alpha = \sqrt{b^2 - c^2}, \quad \beta = \sqrt{c^2 - a^2}, \quad \gamma = \sqrt{a^2 - b^2}.$$

Transform to a new system of coördinates x_1, x_2, x_3, x_4 , by means of the equations

$$\begin{aligned} x_1 &= (c - b) [\alpha\beta x - (b\beta^2 - c\gamma^2)y + iac\alpha\gamma w], \\ x_2 &= (b + c) [\alpha\beta x - (b\beta^2 + c\gamma^2)y + iac\alpha\gamma w], \\ x_3 &= (a + c) [\alpha x - b\beta y + c\gamma z], \\ x_4 &= (c - a) [\alpha x - b\beta y - c\gamma z]. \end{aligned}$$

With respect to this new system, the coördinates of the six chosen nodes are $(1, 0, 0, 0)$, $(0, 1, 0, 0)$, $(0, 0, 1, 0)$, $(0, 0, 0, 1)$, (e_1, e_2, e_3, e_4) , (e_2, e_1, e_4, e_3) , where

$$\begin{aligned} e_1 &= \beta (b^2 - c^2) (c - a), & e_3 &= (a^2 - c^2) (c + b), \\ e_2 &= \beta (b^2 - c^2) (c + a), & e_4 &= (a^2 - c^2) (c - b). \end{aligned}$$

These six points form an involution of the kind described. (See *Annals of Mathematics*, vol. 11, p. 159.)

NOTE ON INTEGRATING FACTORS.

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If the differential equation

$$X_1 dx_1 + X_2 dx_2 + \cdots + X_n dx_n = 0, \quad n \equiv 3, \quad (\text{A})$$

be integrable, and if $u = \text{constant}$ be the integral of this equation, then, as is well known, there exists a function M such that

$$du \equiv MX_1 dx_1 + MX_2 dx_2 + \cdots + MX_n dx_n.$$

And as

$$\frac{\partial u}{\partial x_1} \equiv MX_1, \quad \frac{\partial u}{\partial x_2} \equiv MX_2, \quad \dots \quad \frac{\partial u}{\partial x_n} \equiv MX_n,$$