

sets. That same statement could be made, of course, about the entire book. We are among those who are applauding.

## REFERENCES

1. R. V. Benson, *Euclidean geometry and convexity*, McGraw-Hill, New York, 1966.
2. H. G. Eggleston, *Convexity*, Cambridge Univ. Press, Cambridge, England, 1966.
3. B. Grünbaum, *Convex polytopes*, Wiley, 1967.
4. P. C. Hammer and Andrew Sobczyk, *Planar line families*.I, Proc. Amer. Math. Soc. 4 (1953), 226–233.
5. P. J. Kelly and M. L. Weiss, *Geometry and convexity*, Wiley, New York, 1979.
6. L. A. Lyusternik, *Convex figures and polyhedra*, Dover, New York, 1963.
7. A. W. Roberts and D. E. Varberg, *Convex functions*, Academic Press, New York, 1973.
8. R. T. Rockafellar, *Convex analysis*, Princeton Univ. Press, Princeton, New Jersey, 1970.
9. F. A. Valentine, *Convex sets*, McGraw-Hill, New York, 1964.
10. I. M. Yaglom and V. G. Boltyanskii, *Convex figures*, Holt, Rinehart, and Winston, New York, 1961.

A. W. ROBERTS

D. E. VARBERG

BULLETIN (New Series) OF THE  
AMERICAN MATHEMATICAL SOCIETY  
Volume 8, Number 2, March 1983  
©1983 American Mathematical Society  
0273-0979/82/0000-0977/\$01.75

*Counterexamples in topological vector spaces*, by S. M. Khaleelulla, Lecture Notes in Math., vol. 936, Springer-Verlag, Berlin and New York, 1982, xxi + 179 pp., \$10.70.

Here is a rule-of-thumb test to identify latent mathematicians: Make an assertion. If the young person tries to prove it, (s)he fails the test; if (s)he tries to find a counterexample, you have a future mathematician on your hands.

Examples are more important than theorems. If you teach me the rules of a game and attempt to develop a theory, I will interrupt to say “Let’s play it once”. A course in groups containing pure theory would allow the conjecture “All groups are commutative” to stand unchallenged—besides failing to educate the students.

The role of examples is educational: the derivative of a specific function, a group with 5 members; but we shall be concerned with those which are always thought of as counter: a nowhere differentiable function, a nonmeasurable set.

Is the earliest known counterexample the book of Job? (Assertion: Holiness brings good fortune.)

What is the role of counterexamples in mathematics? (Are there any in Euclid?) I attempt to list the roles in decreasing order of importance; the “big” examples fall early in my list:

1. To refute widely held beliefs. (A nowhere differentiable continuous function, a series whose sum is discontinuous.)

2. To show the need to work in a more general setting. (A nonsequential limit point.)

3. To show the inadequacy of a definition. (Space-filling curve: what does dimension mean?).