

ON THE STRUCTURE OF MAXIMALLY ALMOST PERIODIC GROUPS

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1. Introduction. A topological group G is said to be maximally almost periodic if the continuous almost periodic functions separate points in G , or equivalently if the continuous finite-dimensional unitary representations of G separate points in G . See [4], or [2, §18]. Throughout this note, we use “*representation*” to mean “*continuous finite-dimensional unitary representation*”. Our purpose here is to announce some results concerning maximally almost periodic (MAP) groups which are independent of the classical theorem of Freudenthal-Weil which states that a locally compact connected group is MAP if and only if it is the direct product of \mathbf{R}^n and a compact group [6, §§30, 31].

The results in this note comprise a portion of the author’s doctoral dissertation. Detailed proofs of these and other results will appear at a later date. The author thanks his thesis advisor, Professor Edwin Hewitt, and Professor Lewis Robertson for all their assistance and encouragement.¹

2. Definitions and notation. Let K be a (Hausdorff but not necessarily locally compact) topological group, G a normal subgroup of K and $T = \{t(x): x \in K\}$ be the group of topological automorphisms of G which are restrictions to G of inner automorphisms of K . Let \hat{K} (and \hat{G} resp.) be the space of equivalence classes of irreducible representations of K (and G resp.). In an investigation of \hat{K} it is natural to consider the action on \hat{G} induced by T . For example, see [1]. Let U be a representation, $U \in \sigma \in \hat{G}$, define $t^*(x)U = U \circ t(x)^{-1}$ and define $t^*(x)\sigma$ to be the equivalence class of $t^*(x)U$. If the set $\{t^*(x)\sigma: t(x) \in T\}$ is finite, then σ is said to be *finitely orbited* by T . Let $F(\hat{G}, T)$ be the set $\{\sigma \in \hat{G}: \sigma \text{ is finitely orbited by } T\}$. The *von Neumann kernel* of a group is the intersection of all kernels of representations of that group.

3. Results.

THEOREM 1. *Let K , G and T be as above. If $U \in \sigma \in \hat{K}$ and if $y \in G$ are such that $U_y \neq I$, then there exists an element of $F(\hat{G}, T)$ which separates*

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