

## RESEARCH PROBLEMS

10. Solomon W. Golomb and Edward C. Posner: *Hypercubes of non-negative integers*.

It is known that if an  $n \times n$  matrix of non-negative integers has the "rook-domain property" then the sum of its entries is at least  $n^2/2$  (see Trans. Inst. Electrical and Electronic Engineers, Information Theory, Vol. IT-10, 1964, p. 2051 for two proofs of this result of Joel N. Franklin and Alfred W. Hales). The *rook-domain property* means the following. The rook-domain of a point in a cartesian product of sets is the set of points all of whose coordinates but at most one agree with the coordinates of the given point. The rook-domain property asserts that the sum of all the entries in the rook-domain of every zero in a  $k$ -dimensional  $n \times n \times \cdots \times n$  hypermatrix of non-negative integers is at least  $n$  (obvious correspondence between hypermatrices and cartesian products defines "rook-domain" here).

**PROBLEM.** Prove that if an  $n^k$  hypermatrix of non-negative integers has the rook-domain property, then the sum of all its  $n^k$  entries is at least  $n^k/k$ .

**REMARKS.** A solution would rule out the existence of certain combinatorial configurations. The result is true for  $k=2$  allowing unequal sides (obvious modification in statement), and is presumably true in higher dimensions for unequal sides. There is a way of looking at the problem which makes it sort of a Fubini Theorem. (Received February 5, 1965.)

11. J. de Groot: *Set theory*.

The number of open sets of a metrizable space is a power of two. Does the same hold for a Hausdorff space or for a compact Hausdorff space? (Received April 1, 1965.)