

symmetric space V (irreducible or not) is again Hermitian symmetric and is isomorphic to V .

PROOF. Since $H^1(V, \theta) = 0$ [2], we see that the set of points $t \in B$ for which V_t is isomorphic to V is an open set in B [3]; it is also closed by Theorem 2.

REFERENCES

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ON THE BEST APPROXIMATION FOR SINGULAR INTEGRALS BY LAPLACE-TRANSFORM METHODS

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1. **Introduction.** Let $f(t)$ be a Lebesgue-integrable function in $(0, R)$ for every positive R . We denote by

$$J_\rho(t) = \rho \int_0^t f(t-u)k(\rho u)du \quad (t \geq 0)$$

a general singular integral with parameter $\rho > 0$ and kernel k having the following property (P): $k(u) \geq 0$ in $0 \leq u < \infty$, $k \in L(0, \infty)$, and $\int_0^\infty k(u)du = 1$.

If we restrict the class of functions $f(t)$ such that $e^{-ct}f \in L_p(0, \infty)$, $1 \leq p < \infty$, for every $c > 0$, and if k satisfies (P), then the following statements hold:

- (i) $J_\rho(t)$ exists as a function of t almost everywhere, $e^{-ct}J_\rho \in L_p(0, \infty)$ for every $c > 0$, and $\|e^{-ct}J_\rho\|_{L_p(0, \infty)} \leq \|e^{-ct}f\|_{L_p(0, \infty)}$;
- (ii) $\lim_{\rho \uparrow \infty} \|e^{-ct}\{f - J_\rho\}\|_p = 0$.

Furthermore, we denote by

$$\hat{f}(s) = \int_0^\infty e^{-st}f(t)dt \quad (s = \sigma + ir, \text{Re } s > 0)$$

the Laplace-transformation of a function f belonging to one of the classes described above, and the Laplace-Stieltjes-transform of a