

author's comments on these papers. For example, it is of interest to note that the first entry in the list is a letter from Gauss to Bessel, dated 18 December 1811, in which there is communicated the substance of Cauchy's theorem and certain consequences of it. [According to the second entry in the list, this was some three years before Cauchy announced his result and fourteen years before he published it.] When one realizes that the author's first papers in this field appeared almost simultaneously with various papers of Goursat and Morera on the subject, one appreciates the author's connection with the development of the field at the turn of the century.

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Altes und Neues über konvexer Körper. By H. Hadwiger. (Elemente der Mathematik von höheren Standpunkte aus. Band III.) Basel, Birkhäuser, 1955. 115 pp. 13.50 Swiss fr.

This small volume, containing less than one hundred pages of actual text, gives an elegant and concise account of convex bodies from the standpoint of the geometry of sets. The general approach is to consider the collection of all convex bodies in ordinary space as themselves forming a metric space \mathcal{C} with convex polyhedra as a dense subset. \mathcal{C} also has algebraic structure, namely addition (the Minkowski sum of convex sets) and multiplication by positive scalars (dilation). On this space the volume V , surface area A , and integral mean curvature M are functionals defined in the first instance for convex polyhedra and then extended to \mathcal{C} . Thus it is unnecessary to make any assumption beyond convexity itself on the class of bodies considered. In this context many questions concerning, for example, the differential geometry of convex surfaces become unnatural; but, on the other hand, the study of the functionals V , F , M and their properties, Steiner's symmetrization, and so on, are briefly and elegantly treated. Thus the author easily proves a theorem of Gross and Lusternik to the effect that by repeated symmetrization it is possible to gradually transform any convex body into a sphere; he proves Steiner's formula $V(A_\rho) = V(A) + \rho F(A) + \rho^2 M(A) + 4\pi\rho^3/3$ for the volume of a convex body A_ρ parallel to A at distance ρ ; and he demonstrates the classical Brunn-Minkowski inequalities: $F^2 - 3MV \geq 0$ and $M^2 - 4\pi F \geq 0$. In this latter connection an interesting discussion is given of the unsolved problem of determining what further inequalities three real numbers V , F , M must satisfy in order to be the values of $V(A)$, $F(A)$, $M(A)$ for some convex body A . The final twenty pages deal in a general fashion with the integral geometry of convex bodies. The book ends with a detailed thirteen page bibliography. Some original results of the author are included, in particular