

voted to the discussion of upper and lower bounds of quadratic functionals and to Friedrichs' analysis of Trefftz's method. In the new addition, the author emphasizes a geometrical approach given by Prager and Synge (*Quarterly of Applied Mathematics* vol. 5 (1947) pp. 241-269). Similar questions were widely discussed by various methods in recent publications, and a part of the literature is mentioned by Courant in one of the longest footnotes of the book. In view of the great and deserved influence of the book, such a footnote cannot be passed over without comment. The footnote states that the theories indicated in §9 have been recently rediscovered and advanced by several authors. Let us emphasize that the word rediscovered is incorrect, since all papers refer either to Trefftz's method or to its analysis by Friedrichs. The purpose of the recent investigations was to simplify the method of Trefftz and to obtain stronger results. Incidentally, the footnote omits a reference to the work of Diaz and Weinstein (see e.g. *Schwarz' inequality and the methods of Rayleigh-Ritz and Trefftz*, *Journal of Mathematics and Physics* vol. 26 (1947) pp. 133-136) which uses an analytic approach. The various methods were recently analyzed by Diaz, *Collectanea Mathematica* vol. 4 (1951) pp. 1-47, specially pp. 41-46, who pointed out the advantages of the analytic method, which yields simpler formulas and more correct results than the geometric procedure.

The tendency of understatement of the work done outside the author's circle reappears in the footnote on page 175, where Lord Rayleigh's contributions to variational methods are evaluated as follows: "Even before Ritz, such ideas were successfully employed by Lord Rayleigh."

The book preserves not only all the high points of the original, but also some of its misprints, which, being by now classical, only add to the pleasure of the reader. It is with great expectations that the reviewer is looking forward to the translation and additions to the second volume.

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Forced oscillations in non-linear systems. By C. Hayashi. Osaka, Nippon Printing and Publishing Co., 1953. 14+164 pp. \$4.50.

This book was written "to provide engineers and physicists with practical knowledge concerning the important subject of non-linear oscillations," in particular forced oscillations governed by non-linear equations of the second order.

The text is divided into two parts; the first concerns the stability of steady state oscillations, whereas the second is devoted to a dis-