

tion of linear functions of ordered dyads $X_{m+1}(\alpha) = \sum x_j \alpha_j \alpha_j$ ($j = 1, 2, \dots, m+1$) with coefficients x_j in a suitable domain D (field F) relatively to any given abstract group G of order $m+1$ ($m = 1, 2, \dots$) represented as a regular group of configurational sets of dyads on $m+1$ elements. Two dyads $\alpha_i \alpha_j$ and $\alpha_k \alpha_l$ are then equivalent if and only if they occur in the same configurational set of dyads. Multiplication is determined by $\alpha_i \alpha_j \times \alpha_k \alpha_l = \alpha_i \alpha_k$ and by the preceding equivalences. Other instances of dyadic representation of linear algebras are given by two examples: 1. $X_2(\alpha) = x_1 \alpha_1 \alpha_1 + x_2 \alpha_2 \alpha_2$ with equivalences $\alpha_1 \alpha_1 = \alpha_2 \alpha_2$, $\alpha_1 \alpha_2 = -\alpha_2 \alpha_1$. 2. $X_4(\alpha) = \sum x_j \alpha_j \alpha_j$ ($j = 1, 2, 3, 4$) with equivalences corresponding to those given by the author (*Math. Ann.* vol. 69 p. 584). In both examples multiplication is determined by $\alpha_i \alpha_j \times \alpha_k \alpha_l = \alpha_i \alpha_k$ and by the associated equivalences. (Received July 11, 1946.)

278. M. C. Sholander: *On the existence of the inverse operation in certain spaces.*

In a set S of elements x, y, \dots which admits a binary operation—here denoted by multiplication—an element a will be called regular if both (i) $ax = ay$ implies $x = y$ and (ii) $xa = ya$ implies $x = y$. An element a will be called proper if for each element b in S there exist unique solutions x and y in S for the equations $ax = b$ and $ya = b$. It is well known that if the multiplication is commutative and associative S can be imbedded in a space S' of the same type in such a way that all elements regular in S are proper in S' . In this paper it is shown the imbedding process can also be carried out in case the multiplication is one satisfying the alternation law $(ab)(cd) = (ac)(bd)$ and in case the regular elements of S are closed under multiplication. Thus if all elements of S are regular, S' is a quasi-group of a type studied, for example, by D. C. Murdoch (*Trans. Amer. Math. Soc.* vol. 49 (1941) pp. 392–409) and R. H. Bruck (*Trans. Amer. Math. Soc.* vol. 55 (1944) pp. 19–52). Various conditions which insure the necessary closure property in S are given in the paper. (Received July 26, 1946.)

279. J. M. Thomas: *Eliminants.*

If $R(a, b)$ denotes the resultant to two polynomials $x(t), y(t)$ whose constant terms are a, b , the polynomial $R(a-x, b-y)$ in the two indeterminates x, y is the *eliminant* $E(x, y)$ of $x(t), y(t)$. This paper (i) proves $E(x, y) = f^k$, where f is an irreducible polynomial and k is a positive integer; (ii) proves $E(x, y)$ is reducible ($1 < k$) if and only if $x(t), y(t)$ are also polynomials in a second parameter which is itself a polynomial of degree at least two in t ; (iii) expresses in terms of $E(x, y)$ algebraic conditions that a single polynomial $y(t)$ be a polynomial in $x(t)$ of degree k , where $1 < k < \deg y$ (these last polynomials have been called by Ritt composite polynomials, *Trans. Amer. Math. Soc.* vol. 23 (1922) pp. 51–66). (Received July 27, 1946.)

280. J. H. M. Wedderburn: *Note on Goldbach's theorem.*

It is shown in this note that, if p and q are primes and $r = (p+q)/2$ is a prime, then $p-q$ is a multiple of 12 unless r has the form $2p-3$ or, when unity is reckoned as a prime, also $r = 2p-1$. The proof is elementary and depends on reducing modulo 12. Similar statements apply if q is replaced by $-q$. (Received July 30, 1946.)

ANALYSIS

281. R. P. Agnew: *Methods of summability which evaluate sequences of zeros and ones summable C_1 .*