

This gives an application of the methods recently discovered by the author to lattice points in the region  $|x^m + y^n| \leq 1$  where  $m = p/q > 4$  and  $p, q$  are odd integers. (Received April 9, 1945.)

#### ANALYSIS

##### 109. R. P. Agnew: *Tauberian theorems for Nörlund summability.*

It is shown that a Tauberian theorem for Nörlund summability given by R. P. Cesco (Universidad Nacional de La Plata, Publicaciones de la Facultad de Ciencias Fisicomatematicas (2) vol. 4 (1944) pp. 443-445) and more general theorems are implied by familiar Tauberian theorems for Abel summability. (Received May 14, 1945.)

##### 110. R. H. Cameron: *Some examples of Fourier-Wiener transforms of analytic functionals.*

Let  $F[x] = F[x(\cdot)]$  be a functional which is defined throughout the space  $K$  of complex continuous functions  $x(t)$  defined on  $0 \leq t \leq 1$  and vanishing at  $t=0$ , and let  $F$  possess the property that  $F[x+iy]$  is Wiener summable in  $x$  over  $C$  for each fixed  $y(\cdot)$  in  $K$ . ( $C$  is the subspace of all real functions in  $K$ .) Then the functional  $G[y] = \int_C^w F[x+iy] d_w x$  is called the Fourier-Wiener transform of  $F(x)$ . Examples are given of various functionals  $F(x)$  which have the property that the transforms of their transforms exist and equal  $F(-x)$ . The fact that there exist extensive classes of functionals having this property is proved in a paper by W. T. Martin and the author. (Received May 9, 1945.)

##### 111. R. H. Cameron and W. T. Martin: *Fourier-Wiener transforms of analytic functionals.*

Let  $K$  be the space of all continuous complex functions  $x(t)$  defined on  $0 \leq t \leq 1$  which vanish at  $t=0$ , let  $C$  be the subset of all real functions of  $K$ , and let  $F[x]$  be a functional defined on  $K$ . Then, as defined by one of the authors in another paper,  $G(y) = \int_C^w F(x+iy) d_w x$  is called the Fourier-Wiener transform of  $F(x)$  if it exists for all  $y$  in  $K$ . The purpose of the present paper is to exhibit three extensive classes of functionals which are taken into themselves in a one-to-one manner by the Fourier-Wiener transformation in such a way that the inverse transformation is  $F(x) = \int_C^w G(y-ix) d_w y$ . In particular, this property is enjoyed by the class  $E_m$  of functionals  $F(x)$  which are mean continuous, of mean exponential type, and "entire," that is, continuous in the topology defined by root mean square distance between functions, bounded by  $A \exp [B \int_0^1 x(t)^2 dt]^{1/2}$ , and "entire" in the sense that  $F(x+\lambda y)$  is entire in  $\lambda$  for all  $x$  and  $y$  in  $K$ . (Received May 9, 1945.)

##### 112. Nelson Dunford and Robert Schatten: *On the associate and conjugate space for the direct product of Banach spaces.*

The direct product  $E_1 \otimes_N E_2$  of two Banach spaces  $E_1, E_2$  (Trans. Amer. Math. Soc. vol. 53 (1943) pp. 195-217), which naturally depends on the norm  $N$ , determines uniquely an "associate space"  $\bar{E}_1 \otimes_{\bar{N}} \bar{E}_2$  ( $\bar{N}$  is the norm "associate" with  $N$ ) and a conjugate space  $\bar{E}_1 \otimes_N E_2$ . It is shown that for a "natural crossnorm,"  $\bar{L} \otimes_{\bar{N}} \bar{L}$  is a proper subset of  $\bar{L} \otimes_N \bar{L}$ . Similarly, for a "natural crossnorm,"  $\bar{l} \otimes_{\bar{N}} \bar{l}$  is a proper subset of  $\bar{l} \otimes_N \bar{l}$ . A related example of a non-reflexive crossspace  $E_1 \otimes_N E_2$  is constructed, for which  $E_1, E_2$ , and  $N$  are all reflexive. (Received April 23, 1945.)

##### 113. Herbert Federer: *Coincidence functions and their integrals.*