

Let D_{H_2} denote a domain containing H_2 such that $\overline{D_{H_2}} \cdot \overline{(K + D_{K_1})} = 0$. Let D_{K_2} denote a domain containing K_2 and such that $\overline{D_{K_2}} \cdot \overline{(H + D_{H_1} + D_{H_2})} = 0$. This process may be continued and $D_H = \sum D_{H_n}$ and $D_K = \sum D_{K_n}$ are two mutually exclusive domains covering H and K respectively.

THE UNIVERSITY OF TEXAS

ON AN INTEGRAL EQUATION WITH AN ALMOST PERIODIC SOLUTION

BY B. LEWITAN

We assume that the function $f(x)$ is almost periodic in the sense of H. Bohr and that the functions $E(\alpha)$, $\alpha E(\alpha)$ are absolutely integrable in $[-\infty, \infty]$.

THEOREM. *If all real zeros of the function*

$$\gamma(\alpha) = \frac{1}{2\pi} \int_{-\infty}^{\infty} E(u) e^{-i\alpha u} du$$

have integer multiplicities and only two limit points ∞ , α^ , then every solution $\phi(x)$ of the equation*

$$(1) \quad \int_{-\infty}^{\infty} E(\xi - x) \cdot \phi(\xi) d\xi = f(x)$$

which is uniformly continuous and bounded in $[-\infty, \infty]$ is almost periodic.

PROOF. Without loss of generality we may assume that the finite limit point α^* has the value 0; otherwise we multiply equation (1) by $e^{-i\alpha^*x}$.

Putting

$$f_n(x) = \frac{3}{2\pi} \int_{-\infty}^{\infty} f\left(x + \frac{2u}{n}\right) \frac{\sin^4 u}{u^4} du,$$

we obtain

$$\int_{-\infty}^{\infty} E(\xi) \phi_n(\xi + x) d\xi = f_n(x),$$