

$$[(5), (9)] \quad r \rightarrow s. = .i \quad (6)$$

$$[(4), (6)] \quad p \rightarrow q. = .r \rightarrow s \quad (7)$$

$$[11.03] \quad (7) = (1)(2) \quad (8)$$

$$[(7), (8)] \quad (1)(2) \quad (9)$$

$$[11.2] \quad (1)(2) \rightarrow (1) \quad (10)$$

$$[12.17] \quad (1)(2) \rightarrow (2) \quad (11)$$

$$[(9), (10)] \quad (1)$$

$$[(9), (11)] \quad (2) .$$

The paradox stated above is a particular case of Theorem 10, and therefore requires no further proof.

NATIONAL WU-HAN UNIVERSITY,  
WUCHANG, CHINA

## THE BETTI NUMBERS OF CYCLIC PRODUCTS

BY R. J. WALKER

1. *Introduction.* In a recent paper† M. Richardson has discussed the symmetric product of a simplicial complex and has obtained explicit formulas for the Betti numbers of the two- and three-fold products. Acting on a suggestion of Lefschetz, we define a more general type of topological product and apply Richardson's methods to compute the Betti numbers of a certain one of these, the "cyclic" product.

2. *Basis for  $m$ -Cycles of General Products.* Let  $S$  be a topological space and  $G$  a group of permutations on the numbers  $1, \dots, n$ . The *product of  $S$  with respect to  $G$* ,  $G(S)$ , is the set of all  $n$ -tuples  $(P_1, \dots, P_n)$  of points of  $S$ , where  $(P_{i_1}, \dots, P_{i_n})$  is to be regarded as identical with  $(P_1, \dots, P_n)$  if and only if the permutation  $(\begin{smallmatrix} 1 & \dots & n \\ i_1 & \dots & i_n \end{smallmatrix})$  is an element of  $G$ . A neighborhood of  $(P_1, \dots, P_n)$  is the set of all points  $(Q_1, \dots, Q_n)$  for which  $Q_i$  belongs to a fixed neighborhood of  $P_i$ . It is not difficult to verify that the

† M. Richardson, *On the homology characters of symmetric products*, Duke Mathematical Journal, vol. 1 (1935), pp. 50-69. We shall refer to this paper as R.