

$B - B \cdot T = H_2 + H_1 \cdot B$ , and  $H_2 \cdot C = 0$ , contrary to the lemma.

6. *Conclusion.* In conclusion attention is called to the desirability of clearing up, in the general case, the possibilities for the power of the class of all sets  $[H(N)]$  in a compact space for any system  $T$ , such as has already been done by Mazurkiewicz and Alexandroff (see papers in *Fundamenta Mathematicae*, vols. 19 and 20) in the special case of the dimensional components. Also a more detailed study of the structure of continua  $M$  of varying degrees of connectivity and local connectivity with respect to the sets  $H(N)$ , in particular in the case\* considered in §5, would be highly desirable.

THE JOHNS HOPKINS UNIVERSITY

## INTEGRAL DOMAINS OF RATIONAL GENERALIZED QUATERNION ALGEBRAS†

BY A. A. ALBERT

1. *Introduction.* We shall consider generalized quaternion algebras

$$Q = (1, i, j, ij), \quad ji = -ij, \quad i^2 = \alpha, \quad j^2 = \beta,$$

over the field  $R$  of all rational numbers. It is easily shown that, by a trivial transformation on the basis of  $Q$ , we may take  $\alpha$  and  $\beta$  to be integers without square factors.

Of great interest in the theory of algebras  $Q$  are the integral sets of  $Q$ . L. E. Dickson‡ has called a set  $S$  of quantities of  $Q$  an integral set if  $S$  satisfies the following postulates:

$R$ : The quantities of  $S$  have minimum equations with ordinary whole number coefficients and leading coefficient unity.

$C$ :  $S$  is closed under addition, subtraction, and multiplication.

$U$ :  $S$  contains 1,  $i$ ,  $j$ .

$M$ :  $S$  is maximal.

---

\* A further study of this case is made in the author's paper *Cyclic elements of higher order*, to appear in the *American Journal of Mathematics*, vol. 56 (1934).

† Presented to the Society, June 19, 1933.

‡ See Dickson's *Algebren und ihre Zahlentheorie*, pp. 154–197, for his theory as well as references to the work of Latimer and Darkow. See also Latimer's later paper, *Transactions of this Society*, vol. 32 (1930), pp. 832–846.