

I shall close with one further observation as to the properties of the set M . Mazurkiewicz calls* a set M quasi-connected if for every point m of M there corresponds a positive number λ such that there does not exist any division of M into two mutually separated sets M_1 and M_2 such that M_1 contains m and the diameter of M_1 is less than λ . He gives† an example of a quasi-connected set which contains no true quasi-components. That the set M constructed above is another example of such a set is easily shown; indeed, the value of λ may be taken *uniformly* equal to unity for all points of M .

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A SIMPLE METHOD FOR NORMALIZING TCHEBY-
CHEFF POLYNOMIALS AND EVALUATING
THE ELEMENTS OF THE ALLIED
CONTINUED FRACTIONS‡

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1. *Introduction.* Consider a system

$$(1) \quad P_n(x), \quad (n = 0, 1, 2, \dots),$$

of orthogonal, but not normal, Tchebycheff polynomials corresponding to a given (finite or infinite) interval (a, b) with the characteristic function $p(x)$. The corresponding *normalized* system of polynomials will be denoted by

$$(2) \quad \phi_n(p; x) \equiv \phi_n(x) = a_n(p) [x^n - S_n(p)x^{n-1} + \dots],$$

$$(n = 0, 1, \dots, a_n > 0).$$

We have, then,

$$(3) \quad \int_a^b p(x) \phi_m(x) \phi_n(x) dx = \begin{cases} 0, & m \neq n, \\ 1, & m = n. \end{cases}$$

* *Sur les ensembles quasi-connexes*, Fundamenta Mathematicae, vol. 2 (1921), pp. 201-205.

† Loc. cit.

‡ Presented to the Society, April 16, 1927.