

## SHORTER NOTICES

*An Elementary Treatise on Frequency Curves and their Application in the Analysis of Death Curves and Life Tables.* By Arne Fisher. Translated from the Danish by E. A. Vigfusson. With an introduction by Raymond Pearl. American Edition. New York, Macmillan, 1922. xv + 244 pp.

This work is divided into two chapters. The first, "An Introduction to the Theory of Frequency Curves", is practically the same as Chapters XIV–XVIII of *Mathematical Theory of Probabilities*, by the same author. This chapter takes up the treatment of frequency curves associated with the names of Laplace, Poisson, Charlier, Thiele and Gram, and serves as the theoretical introduction to the second chapter entitled "The Human Death Curve." In this chapter the author presents a method of constructing mortality curves from death lists by age and cause without knowledge of the number exposed to risk. In the United States this method has been received with various degrees of enthusiasm—from that of the extremely eulogistic introduction to the book down to utter condemnation by several well known actuaries whose views carry much weight. It is an axiom in actuarial science, often repeated and emphasized, that a mortality curve cannot be constructed from death lists alone. Some criticisms seem to imply that Fisher had done just this thing and a man of straw is created and warmly pelted. But he does not claim to get a mortality curve from death lists alone. It is true that he does not have the exposed to risk, but he has a substitute in something biologists and physicians have told him about the frequency distribution of deaths according to age from various classes of causes.

Dispensing with actuarial technicalities, the problem in the language of the theory of probabilities is as follows:

A bag contains a large number of black and white balls. Each ball has a number stamped upon it which may be any integer from 0 to 105. The black balls are also stamped with one of the letters *a, b, c, d, e, f, g, h*. Balls are drawn from the bag one at a time and replaced. A record is kept of the numbers and letters on the black balls, but no attention is paid to the numbers on the white balls. Later it is found desirable to construct a table of  $d_x/l_x$ , where  $d_x$  is the number of black balls, marked with the number  $x$ , and  $l_x$  is the total number of observed balls so marked. It is of course impossible to make such a table from the black ball records. But there is available information about the distribution of the balls in other bags