

THE INVARIANTS OF FORMS  
UNDER THE BINARY LINEAR HOMOGENEOUS  
GROUP  $G_6$  MODULO  $2^*$

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1. *Introduction.* The transformation of an arbitrary binary quantic whose coefficients are written without binomial multipliers,

$$(1) \quad f = (a_0, \dots, a_m) (x_1, x_2)^m = \prod_{i=0}^m (r_2^{(i)} x_1 - r_1^{(i)} x_2),$$

by the formulas

$$T: \quad x_1 = \lambda_1 x'_1 + \mu_1 x'_2, \quad x_2 = \lambda_2 x'_1 + \mu_2 x'_2,$$

in which  $\lambda_i, \mu_j$  are such residues of a prime  $p$  that  $T$  ranges over the total group  $G$  of order  $(p^2 - p)(p^2 - 1)$ , leads to the formal modular concomitant system of  $f$ . For various reasons  $p = 2$  gives rise to exceptions in this theory; thus quadratic congruence theory becomes very special when  $p = 2$ , and also certain types of modular concomitants exist† for the even modulus that do not exist for  $p > 2$ .‡

2. *Analogies.* It is a known result of algebraic (non-modular) invariant theory that every concomitant of (1) is a polynomial in determinants of two types, viz.  $(r^{(i)} r^{(j)})$ ,  $(r^{(i)} x)$ , i. e., linear forms themselves and resultants of pairs of them. Also the complete system of covariants of any number of quadratic quantics,

$$(2) \quad f_1 = (a_0, \dots, a_2) (x_1, x_2)^2, \dots, f_r = (l_0, \dots, l_2) (x_1, x_2)^2,$$

is a set of concomitants that can be formed as transvectants of forms  $f_i$  taken in pairs.§ The dyadic combinations therefore furnish the complete seminvariant systems, also, but for the invariants it is found that the eliminants of the triadic combinations of the forms  $f_1, \dots, f_r$  are to be added.

\* Presented to the Society, December 28, 1923.

† TRANSACTIONS OF THIS SOCIETY, vol. 19 (1918), p. 110.

‡ Dickson, *The Madison Colloquium Lectures*, Lecture III, p. 33-64.

§ Grace and Young, *Algebra of Invariants*, 1903, p. 161.