

where  $\psi$  is an arbitrary function.

From (5) it is evident that if  $A_{ij}$  are defined as the components of the curl of covariant vector, then (2) are necessarily satisfied; but (2) is not a sufficient condition. That this condition is not sufficient was overlooked by me in a recent paper,\* and my conclusions in § 5 are not correct. In fact, the skew-symmetric tensor there defined by  $S_{ij}$  is given by

$$S_{ij} = \frac{\partial \Gamma_{\alpha j}^{\alpha}}{\partial x^i} - \frac{\partial \Gamma_{\alpha i}^{\alpha}}{\partial x^j},$$

and the functions  $\Gamma_{\alpha i}^{\alpha}$  and  $\Gamma'_{\alpha i}$  in two sets of coordinates are in the relation

$$\Gamma'_{\alpha i} = \Gamma_{\alpha j}^{\alpha} \frac{\partial x^j}{\partial x'^i} + \frac{\partial}{\partial x'^i} \log \Delta,$$

where  $\Delta$  is the Jacobian of the transformation.

PRINCETON UNIVERSITY

## A NEW GENERALIZATION OF TCHEBYCHEFF'S STATISTICAL INEQUALITY

BY B. H. CAMP

1. *Introduction.* If  $f(x)$  is any frequency distribution, and  $s$  its standard deviation, the symbol  $P(\lambda s)$  may be used to represent the probability that a datum drawn from this distribution will differ from the mean value by as much as  $\lambda s$ , numerically. For the solution of various statistical problems it is desirable to have a formula which will measure  $P(\lambda s)$  when  $f(x)$  is only partially known. A case of practical importance occurs when  $f(x)$  represents the distribution of values of a statistical constant determined by sampling from a known distribution, such a constant as, for example, a mean value, or a coefficient of correlation. In such cases it is usually difficult or impossible to find the complete distribution  $f(x)$ , but quite feasible to find its lower moments. Tchebycheff's well known inequality is:  $P(\lambda s) \leq 1/\lambda^2$ . It has been general-

\* PROCEEDINGS OF THE NATIONAL ACADEMY, vol. 8 (1922), p. 236.