

$$\xi_2 = \pm \frac{1}{2} \left\{ -2 \frac{\left(\frac{\partial g}{\partial \xi}\right)_0}{g_0} \right\} h^2 + \epsilon,$$

$$\xi_1 = \pm \frac{1}{2} \left\{ -\frac{1}{3g_0} \left[ \left(\frac{\partial g}{\partial \xi}\right)_0 + 4\omega^2 \sin \phi_0 \cos \phi_0 \right] \right\} h^2 + \epsilon',$$

where  $\epsilon$  and  $\epsilon'$  are infinitesimals of order higher than that of  $h^2$ . In order to remove the ambiguity in sign let us observe that since the latitude  $\phi$  lies between  $-90^\circ$  and  $+90^\circ$ , it follows that  $\cos \phi > 0$ , and therefore, by relation (40),  $(\partial j / \partial s) / j$  and  $d^2y/dx^2$  are either both positive or both negative. Hence it follows from (45) and Theorem 8 that for the curve  $d$ ,  $-(\partial g / \partial \xi)_0 / g_0$  and  $(d^2z/d\tau^2)_0$  are either both positive or both negative; and from (50) and Theorem 9 that for the curve  $c'$ ,  $-1/g_0 \{ (\partial g / \partial \xi)_0 + 2\omega^2 \sin 2\phi_0 \}$  and  $(d^2z/d\tau^2)_0$  are either both positive or both negative. Furthermore, we assumed  $\xi_1$  and  $\xi_2$  to be positive toward the equator. Consequently if for definiteness we suppose (as shown in Fig. 5) that for curve  $d$ ,  $(d^2z/d\tau^2)_0 > 0$  and for curve  $c'$ ,  $(d^2z/d\tau^2)_0 < 0$ , it follows that  $\xi_2 = -P_1T < 0$  and  $\xi_1 = TC' > 0$ . Therefore in the above expressions for  $\xi_2$  and  $\xi_1$  the lower signs must be used and thus we have

$$(52) \quad \xi_2 = \frac{\left(\frac{\partial g}{\partial \xi}\right)_0}{g_0} h^2,$$

$$(53) \quad \xi_1 = \left\{ 2\omega^2 \sin 2\phi_0 + \left(\frac{\partial g}{\partial \xi}\right)_0 \right\} \frac{h^2}{6g_0},$$

to terms of order not higher than the second in  $h$ , whence

$$(54) \quad \text{S.D.} = \xi_1 - \xi_2 = \left\{ 2\omega^2 \sin 2\phi_0 - 5 \left(\frac{\partial g}{\partial \xi}\right)_0 \right\} \frac{h^2}{6g_0},$$

which is formula (I).

## NOTE ON SOLVABLE QUINTICS.

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(Read before the American Mathematical Society, January 2, 1915.)

THE substance of the following paper was included several years ago in my university lecture course on the theory of