

Further, formula (9) of § 11 becomes for $q = m - 2$

$$\begin{vmatrix} i_1 i_2 \cdots i_{m-2} \\ j_1 i_2 \cdots j_{m-2} \end{vmatrix} A = D^{m-3} \begin{vmatrix} i_{m-1} i_m \\ j_{m-1} j_m \end{vmatrix} a.$$

Hence the transformation (12) takes the form*

$$(12_1) \quad W_{i_{m-1} i_m} = D^{\frac{m-4}{2}} \sum_{j_{m-1} j_m}^{1, \dots, m} \begin{vmatrix} i_{m-1} i_m \\ j_{m-1} j_m \end{vmatrix} a W_{j_{m-1} j_m}.$$

18. We may enunciate the results proven in §§ 16-17 for the individual transformations of the groups concerned :

To any given transformation (a_{ij}) of determinant D of the general m -ary linear homogeneous group G_m , there corresponds a transformation $[a]_{m-2}$ of the $(m-2)^d$ compound $C_{m, m-2}$ which gives rise to a linear transformation upon its system of Pfaffian invariants, viz :

1° : for m odd, the m -ary transformation,

$$\overline{F}'_i = D^{\frac{m-3}{2}} \sum_{j=1}^m a_{ij} \overline{F}_j \quad (i=1, \dots, m),$$

which for $D = 1$, is precisely the given transformation of G_m .

2° . for m even, the $\frac{1}{2}m(m-1)$ -ary transformation (12) or (12₁), where, for $D = 1$, (12₁) belongs to the second compound of G_m , and (12) to the $(m-2)^d$ compound of the $(m-1)^{st}$ compound of G_m .

UNIVERSITY OF CALIFORNIA,
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A SECOND LOCUS CONNECTED WITH A SYSTEM OF COAXIAL CIRCLES.

BY PROFESSOR THOMAS F. HOGGATE.

(Read before the American Mathematical Society at its Fifth Summer Meeting, Boston, August 19, 1898.)

In a paper read before this Society at its Toronto Meeting and published in the BULLETIN for November, 1897, I

* We may verify (12₁) directly, using the method of § 6 for $q=2$. The presence of the factor $D^{\frac{m-4}{2}}$ influences only the transformations A_{ik} . There occurs, however, some difficulty as to signs in passing from the W 's to the F 's. Likewise the results of §§ 11-14 could doubtless be proved by the method of § 6.