

Twisted r -spin potential and Givental's quantization

A. Chiodo¹ and D. Zvonkine²

¹Institut Fourier, UMR du CNRS 5582, Université de Grenoble 1, BP74,
38402, Saint Martin d'Hères, France

`chiodo@ujf-grenoble.fr`

²Institut mathématique de Jussieu, Université Paris VI, 175, rue du
Chevaleret, 75013 Paris, France and; Department of Mathematics,
Stanford University, Building 380, Sloan Hall, Stanford,
California 94305, USA

`zvonkine@math.jussieu.fr`

Abstract

The universal curve $\pi: \bar{\mathcal{C}} \rightarrow \bar{\mathcal{M}}$ over the moduli space $\bar{\mathcal{M}}$ of stable r -spin maps to a target Kähler manifold X carries a universal spin bundle $\mathcal{L} \rightarrow \bar{\mathcal{C}}$. Therefore, the moduli space $\bar{\mathcal{M}}$ itself carries a natural K -theory class $R\pi_*\mathcal{L}$.

We introduce a *twisted* r -spin Gromov–Witten potential of X enriched with Chern characters of $R\pi_*\mathcal{L}$. We show that the twisted potential can be reconstructed from the ordinary r -spin Gromov–Witten potential of X via an operator that assumes a particularly simple form in Givental's quantization formalism.

1 Introduction

In [23] Mumford used the Grothendieck–Riemann–Roch formula to express the Chern characters of the Hodge bundle over the moduli space of stable curves via other tautological classes.