CORRECTION

RANDOM WALK IN A RANDOM ENVIRONMENT AND FIRST-PASSAGE PERCOLATION ON TREES

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The proofs of Proposition 2 and of the first two parts of Theorem 3(ii) are incorrect, although the results themselves are correct. Here are correct proofs.

PROOF OF PROPOSITION 2. Let Π_n be as indicated. Our assumption is that

$$M := \sup_{n} \mathbf{E} \left[\sum_{\sigma \in \Pi_{n}} C_{\sigma}^{x} \right] = \sup_{n} \sum_{\sigma \in \Pi_{n}} p^{|\sigma|} < \infty.$$

Since $x \ge -1$, the inequality between the harmonic mean and the power mean of order x states that for positive numbers a_n , we have

$$\left(\frac{1}{N}\sum_{n=1}^{N}a_{n}^{-1}\right)^{-1} \leq \left(\frac{1}{N}\sum_{n=1}^{N}a_{n}^{x}\right)^{1/x}.$$

Take the *x*th power of both sides, use $a_n := \sum_{\sigma \in \Pi_n} C_{\sigma}$ and the fact that $a_n^x \le \sum_{\sigma \in \Pi_n} C_{\sigma}^x$ since $0 < x \le 1$ to obtain

$$\left(\frac{1}{N}\sum_{n=1}^{N}\left(\sum_{\sigma\in\Pi_{n}}C_{\sigma}\right)^{-1}\right)^{-x} \leq \frac{1}{N}\sum_{n=1}^{N}\left(\sum_{\sigma\in\Pi_{n}}C_{\sigma}\right)^{x} \leq \frac{1}{N}\sum_{n=1}^{N}\sum_{\sigma\in\Pi_{n}}C_{\sigma}^{x}.$$

Now take the expectation to arrive at the bound

$$\mathbf{E}\left[\left(\frac{1}{N}\sum_{n=1}^{N}\left(\sum_{\sigma\in\Pi_{n}}C_{\sigma}\right)^{-1}\right)^{-x}\right] \leq \mathbf{E}\left[\frac{1}{N}\sum_{n=1}^{N}\sum_{\sigma\in\Pi_{n}}C_{\sigma}^{x}\right] \leq M.$$

Fix L > 0. By Markov's inequality, we may deduce that

$$\mathbf{P}\left[\sum_{n=1}^{\infty} \left(\sum_{\sigma \in \Pi_n} C_{\sigma}\right)^{-1} \le L\right] \le \mathbf{P}\left[\sum_{n=1}^{N} \left(\sum_{\sigma \in \Pi_n} C_{\sigma}\right)^{-1} \le L\right]$$
$$= \mathbf{P}\left[\left(\frac{1}{N}\sum_{n=1}^{N} \left(\sum_{\sigma \in \Pi_n} C_{\sigma}\right)^{-1}\right)^{-x} \ge \left(\frac{N}{L}\right)^{x}\right]$$
$$\le M\left(\frac{L}{N}\right)^{x}.$$

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