An Introduction to Continuity, Extrema, and Related Topics for General Gaussian Processes

by Robert J. Adler

This monograph provides a general and abstract introduction to the theory of sample path properties of Gaussian processes based on concepts such as entropy and majorising measures. A generally accessible introduction to majorising measures, the general theory of continuity, boundedness, and suprema distributions for Gaussian processes is presented.

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