

MICROLOCAL HYPO-ANALYTICITY AND EXTENSION OF CR FUNCTIONS

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CONTENTS

INTRODUCTION

I. HYPO-ANALYTIC STRUCTURES

1. Hypo-analytic structures. Definitions
2. The structure bundle and the solutions
3. Local properties of hypo-analytic functions
4. A Fourier transform criterion of hypo-analyticity

II. MICROLOCAL HYPO-ANALYTICITY

1. Hypo-analytic wave-front set in hypo-analytic structures of codimension zero
2. A Fourier transform criterion of microlocal hypo-analyticity in hypo-analytic structures of codimension zero
3. Hypo-analytic structures of arbitrary codimension: characteristic points and traces of distribution solutions on maximally real submanifolds
4. Hypo-analytic wave-fronts set in hypo-analytic structures of arbitrary codimension
5. Standardized local charts and the Levi form
6. A criterion of microlocal hypo-analyticity based on the Levi form

BIBLIOGRAPHY

INTRODUCTION

Since the publication of H. Lewy's paper [12] the question of local holomorphic extension of CR functions defined on submanifolds of \mathbf{C}^m has been studied by a number of mathematicians (to name a few: Andreotti and Hill [1], Hill and Taiani [9], Hunt and Wells [11], Wells [17]).

In Baouendi & Treves [2] (and in [3]; for a systematic and updated description see Treves [16]) it has been shown that such a question is actually relevant for all solutions of a system of equations

$$(*) \quad L_j h = 0, \quad j = 1, \dots, n,$$