

Fourier Ultra-Hyperfunctions Valued in a Fréchet Space

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Introduction

When the theory of Sato-hyperfunctions appeared in 1958, J. Sebastião e Silva attempted to construct a space of ultra-distributions which contains the space \mathcal{S}' of tempered ultra-distributions and the space H' of all distributions of exponential growth and is stable under the Fourier transformation. He defined the space which he named the space of ultra-distributions of exponential type and obtained some important results for one-dimensional case [10].

(On the other hand, he studied the space \mathcal{S}' of tempered ultra-distributions for the one-dimensional space. Hasumi [1] extended the space for the n -dimensional space and obtained some valuable results.)

The n -dimensional case was studied by Y. S. Park and M. Morimoto [11]. We defined the space $Q(C^n)$ which was included and dense in the spaces $H(\mathbb{R}^n)$ and $\mathcal{S}(C^n)$ and stable under the Fourier transformation. The dual space $Q'(C^n)$ of $Q(C^n)$ includes the spaces $H'(\mathbb{R}^n)$ and $\mathcal{S}'(C^n)$. The elements of the dual space $Q'(C^n)$ are called the Fourier ultra-hyperfunctions in the Euclidean n -space.

The extension of the theory of Fourier hyperfunctions in T. Kawai [5] to vector valued case was studied by Y. Ito [2], Y. Ito and S. Nagamachi [3], [4], and other mathematicians.

In this paper, we establish the theory of Fourier ultra-hyperfunctions valued in a Fréchet space.

Our results are roughly as follows. Let $Q_b(T^n(K); K')$ be the space of all continuous functions f on $\mathbb{R}^n + iK$ which are holomorphic in the interior of $\mathbb{R}^n + iK$ and satisfy the estimate:

$$\sup \{ \exp(\langle x, \eta \rangle) |f(z)|; \eta \in K', z \in \mathbb{R}^n + iK \} < \infty ,$$