

On the Mixed Problem for Wave Equation in a Domain with a Corner

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Introduction

The purpose of this paper is to generalize the results in [5] and to obtain the complete results.

We consider mixed problems

$$(I) \quad \left\{ \begin{array}{l} L_1[u] = \frac{\partial^2 u}{\partial t^2} - \frac{\partial^2 u}{\partial x^2} - \frac{\partial^2 u}{\partial y^2} + du = f(t, x, y) \\ u(0, x, y) = u_0(x, y), \quad u_i(0, x, y) = u_i(x, y) \\ B_1[u]|_{x=0} = \left(\frac{\partial u}{\partial x} + b \frac{\partial u}{\partial y} - c \frac{\partial u}{\partial t} + \alpha u \right) \Big|_{x=0} = g_1(t, y) \\ B_2[u]|_{y=0} = \left(\frac{\partial u}{\partial y} + \frac{1}{b} \frac{\partial u}{\partial x} - \frac{c}{b} \frac{\partial u}{\partial t} + \frac{\alpha}{b} u \right) \Big|_{y=0} = g_2(t, x) \\ (t, x, y) \in (\mathbf{R}_+^1)^3 \end{array} \right.$$

$$(II) \quad \left\{ \begin{array}{l} L_1[u] = f(t, x, y) \\ u(0, x, y) = u_0(x, y), \quad u_i(0, x, y) = u_i(x, y) \\ B_3[u]|_{x=0} = \left(\frac{\partial u}{\partial x} + \alpha u \right) \Big|_{x=0} = g_1(t, y) \\ B_4[u]|_{y=0} = \left(\frac{\partial u}{\partial y} + \beta u \right) \Big|_{y=0} = g_2(t, x) \\ (t, x, y) \in (\mathbf{R}_+^1)^3 \end{array} \right.$$

and

$$(III) \quad \left\{ \begin{array}{l} L_2[u] = \frac{\partial^2 u}{\partial t^2} - \frac{\partial^2 u}{\partial x^2} - \frac{\partial^2 u}{\partial y^2} - \frac{\partial^2 u}{\partial z^2} + du = f(t, x, y, z) \\ u(0, x, y, z) = u_0(x, y, z), \quad u_i(0, x, y, z) = u_i(x, y, z) \\ B_5[u]|_{x=0} = \left(\frac{\partial u}{\partial x} + \alpha u \right) \Big|_{x=0} = g_1(t, y, z) \end{array} \right.$$