

On a Full Spectrum Condition for 2-Dimensional Linear Quasi-Periodic Systems

Ichiro TSUKAMOTO

Keio University

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§1. In this paper, we consider the problem concerning linear quasi-periodic systems. Before starting our discussions, we state the following definitions.

DEFINITION 1 ([2, 3]). A real number λ is called a characteristic exponent of the system

$$(1.1) \quad \dot{x} = C(t)x, \quad t \in \mathbf{R}, \quad \dot{} = \frac{d}{dt},$$

if there exists a solution $x(t)$ of (1.1) which satisfies

$$\limsup_{t \rightarrow \infty} t^{-1} \log |x(t)| = \lambda.$$

DEFINITION 2 ([4]). If the number of characteristic exponents of (1.1) is equal to the dimension of (1.1), then we say that (1.1) has full spectrum.

Now, let there be given a linear almost periodic system

$$(1.2) \quad \dot{x} = C(t)x, \quad x \in \mathbf{R}^n.$$

If (1.2) has full spectrum, then it is shown in [1] that (1.2) has a fundamental matrix $X(t)$ of the form

$$X(t) = F(t) \operatorname{diag} \left(\exp \left(\int_0^t d_1(s) ds \right), \dots, \exp \left(\int_0^t d_n(s) ds \right) \right)$$

where $F(t)$ is an almost periodic matrix function and $d_i(t)$ ($i=1, \dots, n$) are almost periodic functions. Also it is shown in [4] that, if (1.2) is especially a linear quasi-periodic system whose coefficient matrix satisfies a nonresonance condition and a smoothness condition and if (1.2) has