

Corrections to "On the Vector Bundles $m\xi_n$ over Real Projective Spaces"

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Here, we shall give corrections to §4 of [3].

p. 11, line 23 and footnote: " $H^{n-1}(X; Z_2)$ " should be " $H^{n-1}(X; Z)$ ".

p. 12, line 29 and p. 13, line 1: " $H^{k-2}(RP^k; Z_2)$ " should be " $H^{k-2}(RP^k; Z)$ ".

P. 13, line 12-line 32: The proof of Theorem 4.4 should be replaced as follows:

PROOF. Case (a). By 2.2, we can write $n\xi_k = (n-k-1) \oplus \eta_1$, where η_1 is the $(k+1)$ -dimensional vector bundle over RP^k . We consider the obstructions for η_1 to have three linearly independent cross-sections.

The primary obstruction is $w_{k-1}(\eta_1)$, which is zero sinbe $\binom{n}{k-1}$ is even.

The secondary one belongs to $H^k(RP^k; \pi_{k-1}(V_{k+1,3}))$, and $\pi_{k-1}(V_{k+1,3})=0$ if $k \equiv 1 \pmod{4}$ by [1].

Therefore, we have $\text{span } \eta_1 \geq 3$ and so $\text{span } (n\xi_k) \geq n-k+2$, which is the first result. Assume $k \geq 8$, and write $n\xi_k = (n-k+2) \oplus \eta_2$, where η_2 is the $(k-2)$ -dimensional vector bundle over RP^k . We consider the obstructions for η_2 to have a non-zero cross-section.

The primary obstruction is the Euler class $X(\eta_2)$ of η_2 , which is zero because $H^{k-2}(RP^k; Z)=0$ for odd k . So, η_2 has a non-zero cross-section over the $(k-2)$ -skeleton of RP^k .

The sacondary one is a coset of

$$(w_2 \otimes 1 + 1 \otimes Sq^2) \cdot H^{k-3}(RP^k; Z)$$

by 4.1 with the above corrections, where the dot operates by η_2 . This group is equal to $H^{k-1}(RP^k; Z_2)$ since $n \equiv 0, k \equiv 1 \pmod{4}$. So, η_2 has a non-zero cross-section over the $(k-1)$ -skeleton of RP^k .

Finally, the third one is a coset of

$$(w_2 \otimes 1 + 1 \otimes Sq^2) \cdot H^{k-2}(RP^k; Z_2)$$

by 4.2, where the dot operates by η_2 , and this group is equal to $H^k(RP^k; Z_2)$ since $n \equiv 0, k \equiv 1 \pmod{4}$.

Therefore, η_2 has a non-zero cross-section over RP^k and the proof is completed.

Case (b). By 2.2, we can write $n\xi_k = (n-k) \oplus \eta$, where η is the k -